

A1 Evaluate the following:

$$\left(\frac{8}{27}\right)^{\frac{1}{3}} \times \left(\frac{49}{100}\right)^0 \times \left(\frac{4}{9}\right)^{-\frac{3}{2}}$$

Write your answer in the form $\frac{a}{b}$ in its simplest form.

Pass on the value of $a - b$.



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A2 *T is the number that you will receive.*

C is the midpoint of the line AB.

C is the point $(T - 2, -2)$, and

B is the point $(T - 1, T + 1)$.

A is the point (a, b) .

Pass on the value of $a - b$.



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A3 *T is the number that you will receive.*

The quadratic equation $2y^2 + (1 - T)y - 6 = 0$ has one positive solution a and one negative solution b .

Pass on the value of $a + 4b$.



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A4 *T is the number that you will receive.*

Rearrange the following equation to make x the subject.

$$y = \frac{(T - 1)x + 2}{x - T}$$

Give your answer in the form $x = \frac{ay + b}{cy + d}$ where $a > 0$.



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B1 A set of five positive integers has:

a mean of 9,
a median of 9, and
a mode of 11.

Pass on the smallest integer in the set.



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B2 *T is the number that you will receive.*

Solve the simultaneous equations

$$\begin{aligned}a + b + c &= 6 \\3a + 2b + c &= T + 4 \\9a + 4b + c &= 3T + 2\end{aligned}$$

Pass on the value of $a + c$.

(Hint: start by subtracting the first equation from each of the other two.)



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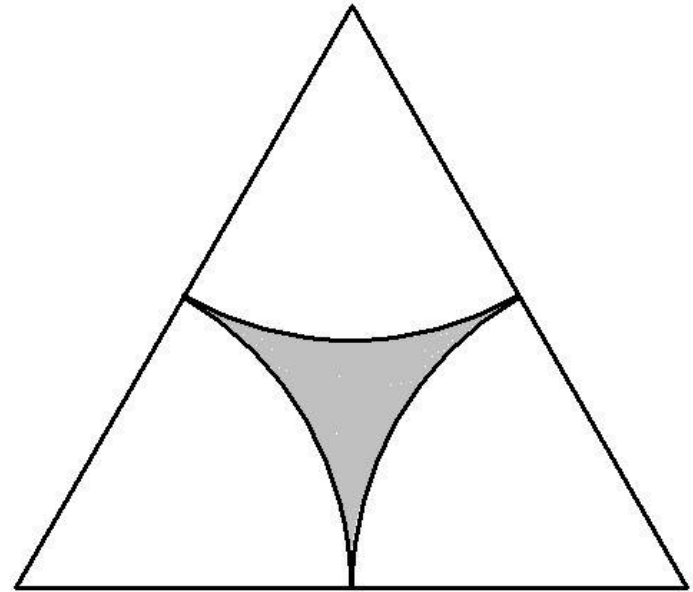


B3 *T is the number that you will receive.*

Three arcs of radius $\frac{T}{2}$ cm are drawn centred at the vertices of an equilateral triangle of side T cm as shown in the diagram.

The area of the shaded region is $a\sqrt{3} - b\pi$ cm².

Pass on the value of $a + b$.



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B4 *T is the number that you will receive.*

The value of $\frac{T\sqrt{12}}{\sqrt{3}-\sqrt{2}}$ can be expressed in the form $a + b\sqrt{6}$, where a and b are integers.

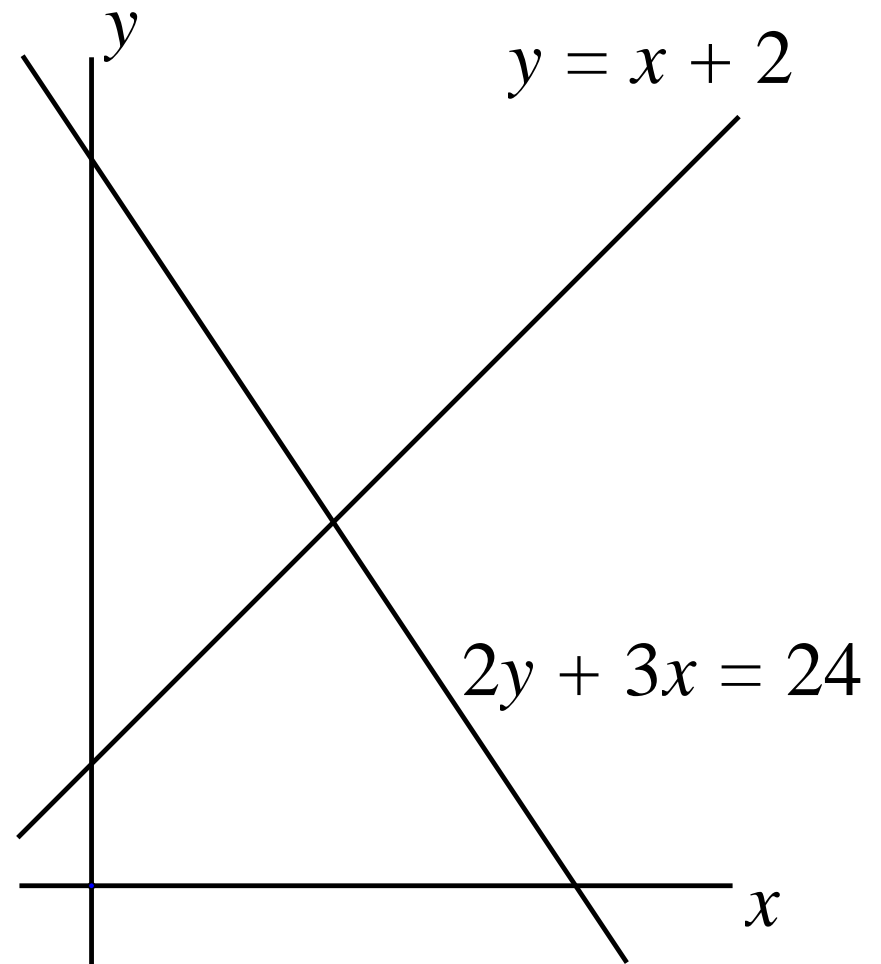
Write down the value of $a - b$.



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C1 A triangle is enclosed by the y axis, the line $y = x + 2$, and the line $2y + 3x = 24$, as shown in the diagram.

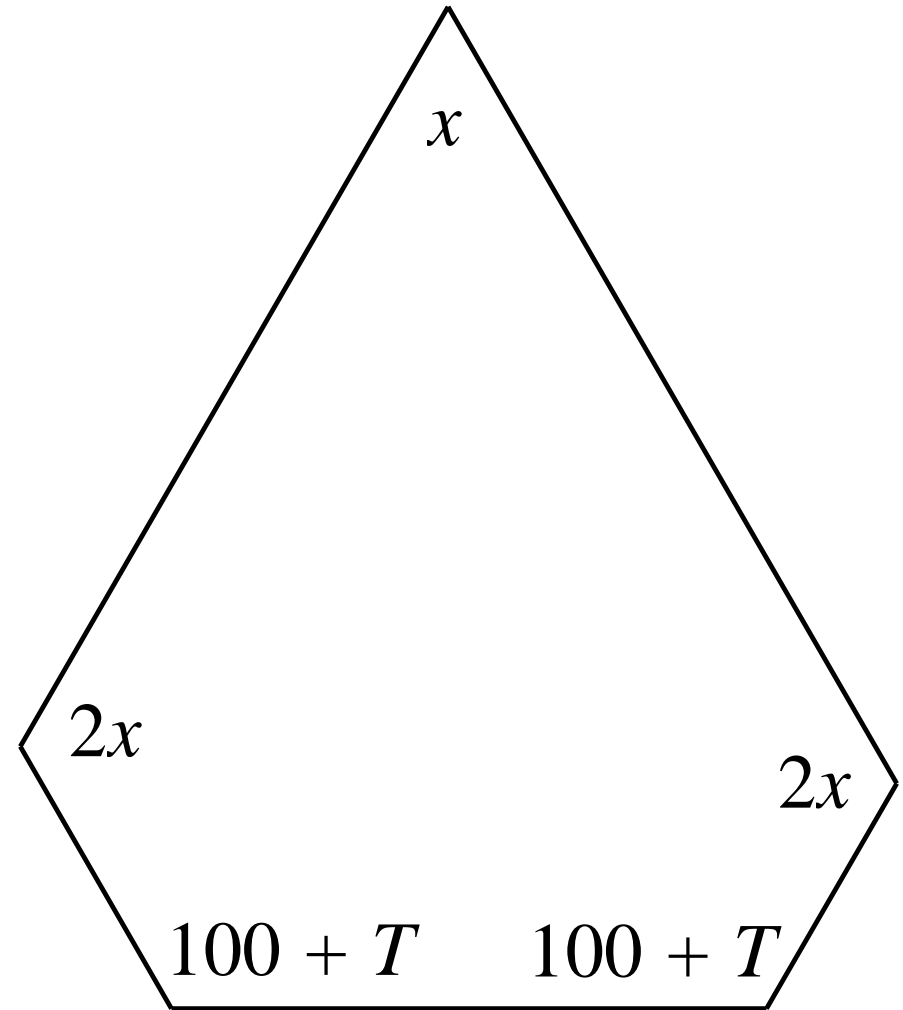


Pass on the area of the triangle.



C2 T is the number that you will receive.

An irregular pentagon has angles $(100 + T)^\circ$, $(100 + T)^\circ$, $(2x)^\circ$, $(2x)^\circ$ and x° as shown in the diagram.



Pass on the value of x .

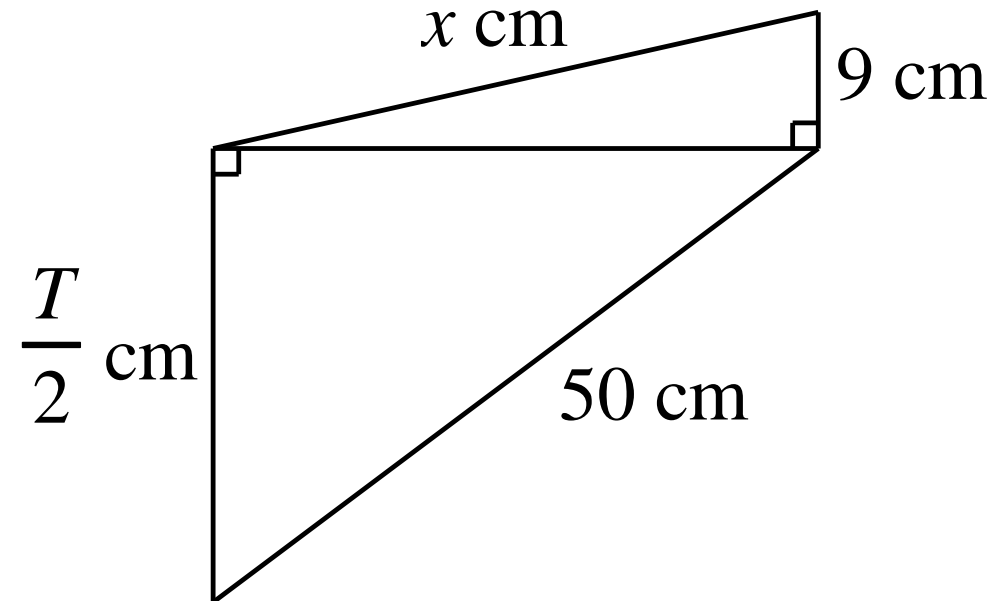


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C3 *T* is the number that you will receive.

The diagram shows two right-angled triangles joined along a common side.

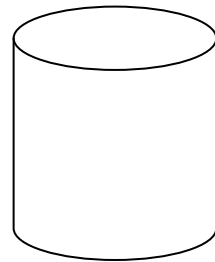


Pass on the value of x .

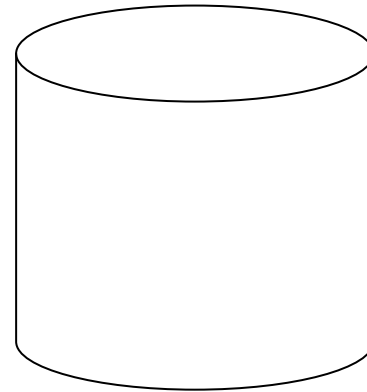


C4 *T is the number that you will receive.*

A sample pot of paint is similar to a regular pot as shown in the diagram. The area of the lid of the sample pot is 54 cm^2 and the area of the lid of the regular pot is 384 cm^2 . The volume of paint in the sample pot is $(6T + 24) \text{ ml}$.



Sample Pot



Regular Pot

Calculate the volume, in litres, of paint in the regular pot.



D1

Let

$$\left(\frac{1}{2}\right)^{y+4} \div \left(\frac{1}{8}\right)^{2y+1} = 512.$$

Pass on the value of y .



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D2 *T is the number that you will receive.*

Paula is going jogging. She jogs 20 km at x km/h and then a further 20 km at $(x + T)$ km/h. Her second 20 km took her 30 minutes less than the first.

Pass on the value of x .

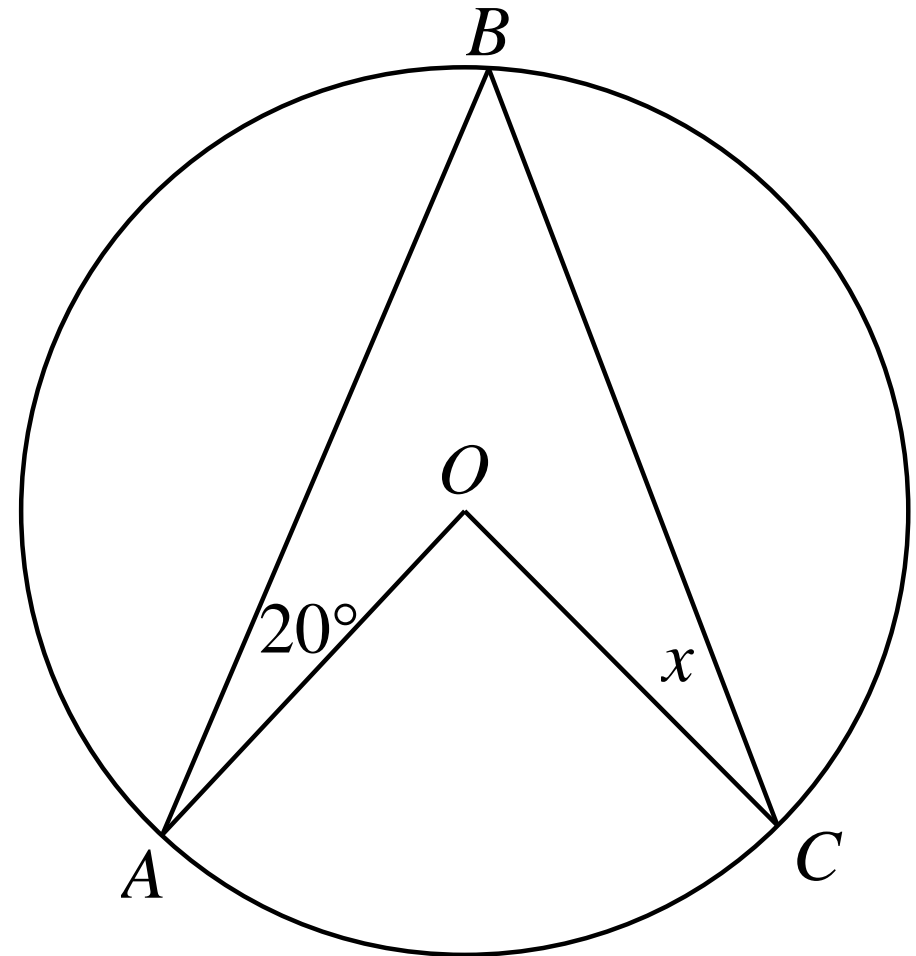


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D3 *T* is the number that you will receive.

In a circle centre *O*, angle *ABC* is $(5T + 4)^\circ$, angle *BAO* is 20° , and angle *BCO* is x° , as shown in the diagram.



Write down
the value of $\frac{1}{6}x$.



D4 *T is the number that you will receive.*

Let

$$x = \sqrt{3 + \sqrt{T + 1}} - \sqrt{3 - \sqrt{T + 1}}$$

Write down the value of x^2 .



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